## CAT－100 Catapult Demonstration

The CAT－100 catapult has six different factors，each of which can be set at three different levels．They are：

| Factor <br> （因子） | Factor Name <br> （因子名稱） | Level <br> （水準） |
| :---: | :--- | :--- |
| A | A：Upright Arm Tension Location <br> （垂直手臂拉力） | 1：Low level，2：Medium level，3：High level <br> （1：低水準，2：中水準，3：高水準） |
| B | B：Projector Elevation <br> （投射高度） | 1：Low level，2：Medium level，3：High level <br> （1：低水準，2：中水準，3：高水準） |
| C | C：Turn Table Position <br> （旋轉盤高度） | 1：Low level，2：Medium level，3：High level <br> （1：低水準，2：中水準，3：高水準） |
| D | D：Pivot Arm Tension Location <br> （中樞手臂拉力） | 1：Low level，2：Medium level，3：High level <br> （1：低水準，2：中水準，3：高水準） |
| E | E：Ball Seat Position <br> （球座位置） | 1：Low level，2：Medium level，3：High level <br> （1：低水準，2：中水準，3：高水準） |
| F | F：Ball Type <br> （球種類） | 1：Foam（yellow），2：Whiffle（white），3：PingPong（orange） <br> （1：黃色球，2：白色球，3：橘色球） |



To test each factor at each level would require a full factorial experiment consisting of 729 different treatment combinations $\left(3^{6}=729\right)$. If the experiment is conducted only using the Level I and II the experiment is reduced to $2^{6}=64$ treatment combinations. This is still a large experiment, hence the need to develop some sort of fractional experiment or Taguchi orthogonal array. (from http://www.qualitytng.com/shop/?page=shop/catdemo)

Different types of fractional factorials can be developed based on the instructor's preferences. The following example is for a one-eighth $\left(2^{6-3}\right)$ fractional factorial with two replications of each treatment. The response variable is the distance the ball is thrown in inches.

| Run <br> Order | A | B | C | D | E | F | Response |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Upright Arm <br> Tension <br> Location | Projector <br> Elevation | Turn Table | Pivot Arm | Ball Seat | Ball Type | Distance |
| 1 | 1 | 1 | 2 | 2 | 1 | 1 |  |
| 2 | 2 | 1 | 2 | 1 | 2 | 1 |  |
| 3 | 1 | 1 | 1 | 2 | 2 | 2 |  |
| 4 | 1 | 2 | 2 | 1 | 1 | 2 |  |
| 5 | 1 | 2 | 1 | 1 | 2 | 1 |  |
| 6 | 1 | 2 | 1 | 1 | 2 | 1 |  |
| 7 | 1 | 1 | 1 | 2 | 2 | 2 |  |
| 8 | 2 | 1 | 1 | 1 | 1 | 2 |  |
| 9 | 2 | 2 | 2 | 2 | 2 | 2 |  |
| 10 | 2 | 2 | 1 | 2 | 1 | 1 |  |
| 11 | 2 | 2 | 2 | 2 | 2 | 2 |  |
| 12 | 2 | 1 | 2 | 1 | 2 | 1 |  |
| 13 | 1 | 1 | 2 | 2 | 1 | 1 |  |
| 14 | 2 | 2 | 1 | 2 | 1 | 1 |  |
| 15 | 1 | 2 | 2 | 1 | 1 | 2 |  |
| 16 | 2 | 1 | 1 | 1 | 1 | 2 |  |

Other Designs

| Full Factorial Design | Factors | Level | Replicates | Runs |
| :--- | :--- | :---: | :---: | :---: |
| $2^{3}$ | 3 (A, D, C) | 2 | 2 | 16 |
| $2^{4}$ | 4 (A, D, E, C) | 2 | 1 | 16 |
| $2^{4}$ | 4 (A, D, E, C) | 2 | 2 | 32 |


| Fractional Factorial Design |  | Factors | Level | Replicates | Runs |
| :--- | :--- | :--- | :---: | :---: | :---: |
| $2^{6-3}(1 / 8$ fraction $)$ | 6 (A, B, C, D, E, F) | 2 | 2 | 16 |  |
| $2^{6-2}(1 / 4$ fraction $)$ | 6 (A, B, C, D, E, F) | 2 | 2 | 32 |  |
| $2^{5-1}(1 / 2$ fraction $)$ | 5 (A, B, C, D, E) | 2 | 2 | 32 |  |

